

# Topics of Mathematics in Final Examination

## Oral Part

### I. Cognitive and Thinking Methods; Sets; Logic; Combinatorics; Graphs

1. *Set Theory*      Basic notions,  
Set operations, properties of operations,  
Applications of sets and set operations in different fields of mathematics  
(number theory, geometry, etc.).
2. *Logic*            Negation, conjunction, disjunction and equivalence and their applications.
3. *Notions, definitions and theorems*  
Interpretation of simple texts of mathematics,  
Exact formulation of definitions and theorems,  
Proper application of necessary and sufficient conditions.
4. *Combinatorics*    Solution of problems.
5. *Graphs*            Basic notions, demonstration of graphs,  
Simple applications.

### II. Number Theory; Algebra

1. *Numbers*            Real numbers,  
Different forms of real numbers,  
Basic operations and their properties,  
Exact value and approximate value, accuracy of calculations and results,  
proper rounding,  
Number systems, 'digits' and their meanings.
2. *Number Theory*    Divisor, multiple, prime number, composite number,  
Fundamental Theorem of Number Theory,  
Decomposition of numbers to product of prime factors,  
Greatest common divisor, Lowest common multiple,  
Simple exercises of divisibility.
3. *Algebraic expressions and operations*  
Operations with algebraic expressions,  
Special binomial products and their applications.
4. *Powers, roots, logarithms*  
Definitions, identities, operations of powers,  
Concept of logarithm, definition, consequences,  
Identities of logarithm and their applications in solution of problems.

### 5. Equations, inequalities

Solution of linear and quadratic equations, inequalities,  
Linear and Quadratic problems,  
Irrational/radical, absolute value equations, inequalities,  
Exponential, logarithmic and trigonometric equations,  
Simultaneous equations,  
Systems of inequalities.

## III. Functions

### 1. Functions, Graphs of functions, transformations of functions

Concept of function, different notations,  
Basic functions: direct proportion, linear, quadratic, radical functions,  
inverse proportion, rational, absolute value functions,  
exponential, logarithmic and trigonometric functions,  
Simple transformations of basic functions:  $f(x) + c$ ,  $f(x + c)$ ,  $c \cdot f(x)$ ,  $f(c \cdot x)$ .

### 2. Characterisation of functions

Domain, range, zeroes, y-intercept, extremes, monotonicity,  
periodicity, parity.

### 3. Sequences

Arithmetic and geometric progressions,  
Arithmetic mean and geometric mean,  
Compound interest.

## IV. Geometry; Analytical Geometry; Trigonometry

### 1. Basic notions, different sets of points

Angle types, angle pairs, measures of angles,  
Locus, special point sets,  
Distance in space,  
Angle of inclination of geometric elements in space.

### 2. Transformations

Properties of transformations,  
Congruent transformations, congruency of figures,  
Basic cases of congruency of triangles,  
Central dilation, similarity,  
Properties of similar figures,  
Application of congruency and similarity in solution of simple problems.

### 3. Shapes of planar geometry

#### a) Triangles

Classification of triangles,  
Definitions of parts of triangles,  
Theorems involving sides, angles and  
special points and lines of triangles,  
Application of theorems and definitions in solution of  
calculation or construction problems.

- b) Quadrilaterals* Types of quadrilaterals and their properties.
- c) Polygons* Equilateral, equiangular and regular polygons,  
Sum of diagonals, sum of interior angles, sum of exterior angles,  
Inscribed and circumscribed circles of regular polygons.
- d) Circle* The circle and its parts,  
Mutual positions of lines and circles.
- 4. Spatial objects* Polyhedra (e.g.: cube, cuboid, tetrahedron, prism, pyramid,  
truncated pyramid),  
Cylinder, cone, frustum, sphere, hemisphere.
- 5. Perimeter, area and volume calculations*  
Perimeter and area formulae of simple planar figures; calculations,  
Area and volume calculations of solids,  
Ratio of perimeter, area and volume of similar planar figures and solids.
- 6. Vectors* Concept of vector,  
Operations with vectors (sum, difference, multiplication by a scalar,  
dot product, linear combination),  
Properties of operations,  
Application of vectors.
- 7. Trigonometry* General definitions of trigonometry functions,  
Simple relations between trigonometry functions and values,  
Law of sines, law of cosines.
- 8. Analytic Geometry*  
Vectors in the coordinate plane, operations with vectors (sum, difference,  
multiplication by a scalar, linear combination),  
Dot product of vectors,  
Different types of equations of lines and circles,  
Mutual positions of lines and circles.

## V. Probability; Statistics

### *1. Descriptive statistics*

Collection, organisation and representation of data,  
Frequency, relative frequency,  
Measures of central tendency: arithmetic mean, weighted average,  
median, mode,  
Variance and standard deviation.

### *2. Probability*

Definition of probability,  
Classic model of probability,  
Sampling with replacement.